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Overview of 3D Object Representations

Emil Praun
(covering for Finkelstein)
Princeton University
COS 426, Fall 2000

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Course Syllabus

- I. Image processing
- II. Rendering
- III. Modeling
- IV. Animation


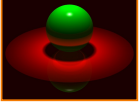
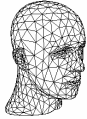



Image Processing
(Rusty Coleman, CS426, Fall99)



Rendering
(Michael Bostock, CS426, Fall99)



Modeling
(Dennis Zorin, CalTech)



Animation
(Angel, Plate 1)

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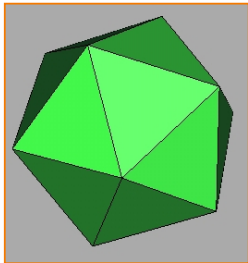
Modeling

- How do we ...
 - Represent 3D objects in a computer?
 - Construct such representations quickly and/or automatically with a computer?
 - Manipulate 3D objects with a computer?

Different methods for different object representations

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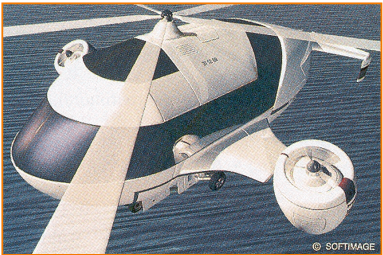
3D Objects



How can this object be represented in a computer?

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3D Objects



This one?

© SOFTIMAGE
H&B Figure 10.46

3D Objects

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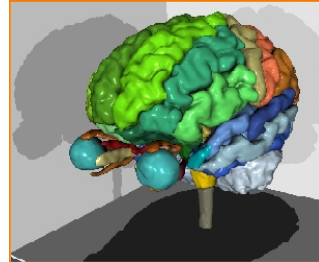


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How about this one?

3D Objects

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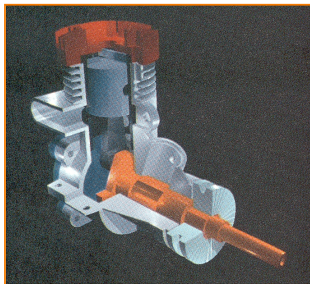


Lorensen

This one?

3D Objects

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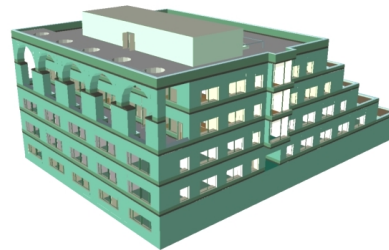


H&B Figure 9.9

This one?

3D Objects

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This one?

Representations of Geometry

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- 3D Representations provide the foundations for
 - Computer Graphics, Computer-Aided Geometric Design, Visualization, Robotics
- They are languages for describing geometry
 - Semantics Syntax
 - values** **data structures**
 - operations** **algorithms**
- Data structures determine algorithms!

3D Object Representations

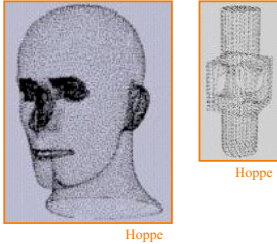
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- Raw data
 - Point cloud
 - Range image
 - Polygon soup
- Surfaces
 - Mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Skeleton
 - Application specific

Point Cloud

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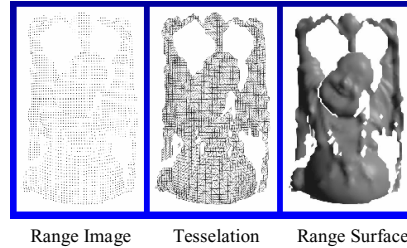
- Unstructured set of 3D point samples
 - Acquired from range finder, computer vision, etc



Range Image

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- Set of 3D points mapping to pixels of depth image
 - Acquired from range scanner

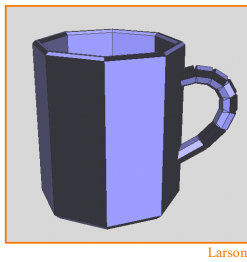


Brian Curless
SIGGRAPH 99
Course #4 Notes

Polygon Soup

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- Unstructured set of polygons
 - Created with interactive modeling systems?



3D Object Representations

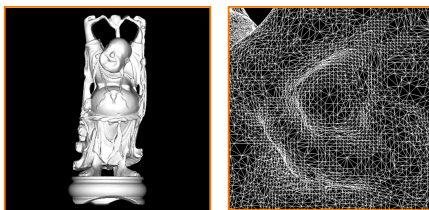
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Mesh

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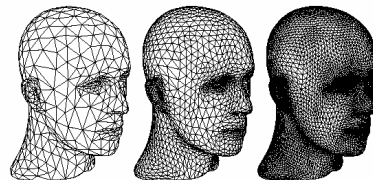
- Connected set of polygons (usually triangles)
 - May not be closed



Subdivision Surface

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- Coarse mesh & subdivision rule
 - Define smooth surface as limit of sequence of refinements

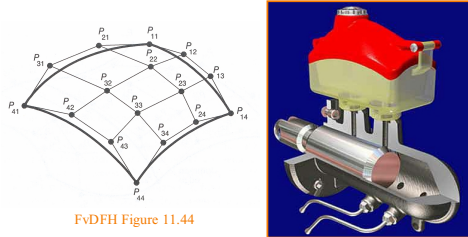


Zorin & Schroeder
SIGGRAPH 99
Course Notes

Parametric Surface

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- Tensor product spline patches
 - Careful constraints to maintain continuity

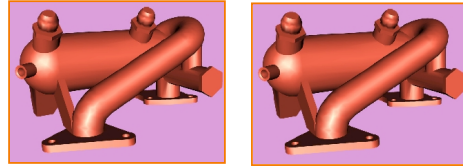


FvDFH Figure 11.44

Implicit Surface

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- Points satisfying: $F(x,y,z) = 0$



Polygonal Model

Implicit Model

Bill Lorensen
SIGGRAPH 99
Course #4 Notes

3D Object Representations

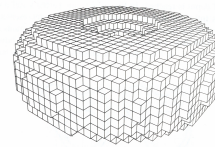
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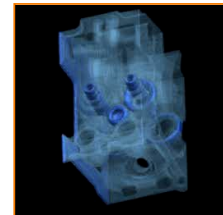
Voxels

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- Uniform grid of volumetric samples
 - Acquired from CAT, MRI, etc.



FvDFH Figure 12.20

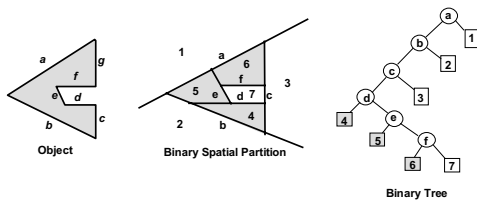


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BSP Tree

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- Binary space partition with solid cells labeled
 - Constructed from polygonal representations

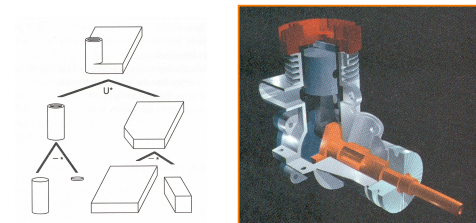


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CSG

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- Hierarchy of boolean set operations (union, difference, intersect) applied to simple shapes



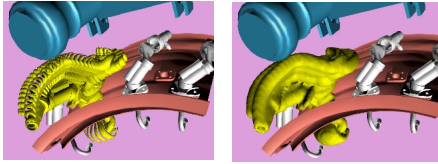
FvDFH Figure 12.27

H&B Figure 9.9

Sweep

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- Solid swept by curve along trajectory



Removal Path

Sweep Model

Bill Lorensen
SIGGRAPH 99
Course #4 Notes

3D Object Representations

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Scene Graph

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- Union of objects at leaf nodes



Bell Laboratories



avalon.viewpoint.com

Skeleton

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- Graph of curves with radii



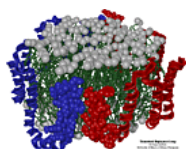
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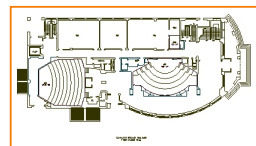
SGI

Application Specific

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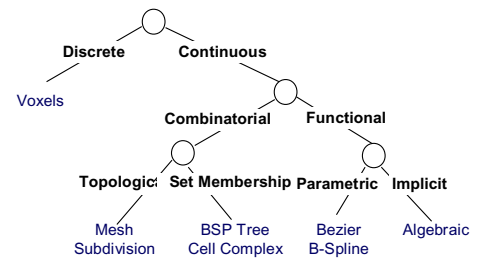
Apo A-1
(Theoretical Biophysics Group,
University of Illinois at Urbana-Champaign)



Architectural Floorplan
(CS Building, Princeton University)

Taxonomy of 3D Representations

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Equivalence of Representations

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- Thesis:
 - Each fundamental representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any fundamental representation!
- Analogous to Turing-Equivalence:
 - All computers today are turing-equivalent, but we still have many different processors

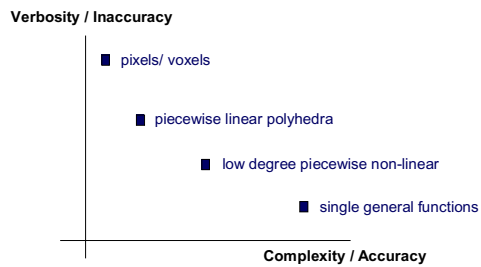
Computational Differences

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- Efficiency
 - Combinatorial complexity (e.g. $O(n \log n)$)
 - Space/time trade-offs (e.g. z-buffer)
 - Numerical accuracy/stability (degree of polynomial)
- Simplicity
 - Ease of acquisition
 - Hardware acceleration
 - Software creation and maintenance
- Usability
 - Designer interface vs. computational engine

Complexity vs. Verbosity Tradeoff

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