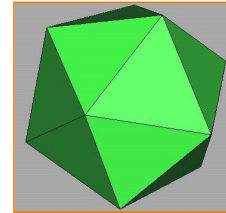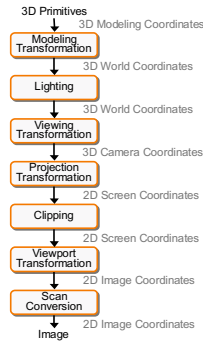# Clipping

Lee Markosian

(covering for Adam Finkelstein)

Princeton University

C0S 426, Fall 2001
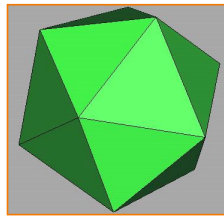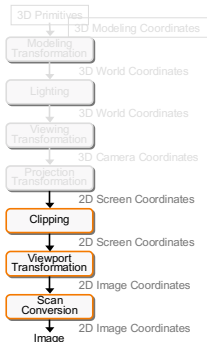

3D Rendering Pipeline (for direct illumination)
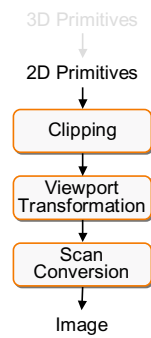

3D Rendering Pipeline (for direct illumination)

2D Rendering Pipeline

3D Primitives

↓

2D Primitives

↓

Clipping — Clip portions of geometric primitives residing outside the window

↓

Viewport Transformation — Transform the clipped primitives from screen to image coordinates

↓

Scan Conversion — Fill pixels representing primitives in screen coordinates

↓

Image

2D Rendering Pipeline

3D Primitives

↓

2D Primitives

↓

Clipping — Clip portions of geometric primitives residing outside the window

↓

Viewport Transformation — Transform the clipped primitives from screen to image coordinates

↓

Scan Conversion — Fill pixels representing primitives in screen coordinates

↓

Image
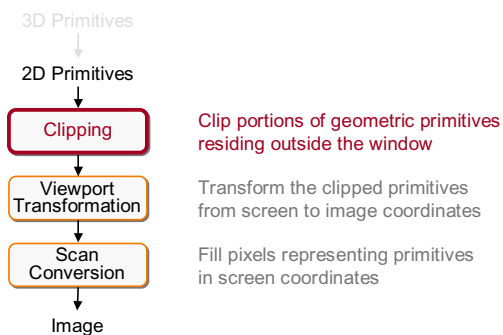
Clipping

- Avoid drawing parts of primitives outside window
  - o Window defines part of scene being viewed
  - o Must draw geometric primitives only inside window

Window

Screen Coordinates

Clipping

- Avoid drawing parts of primitives outside window
  - o Window defines part of scene being viewed
  - o Must draw geometric primitives only inside window
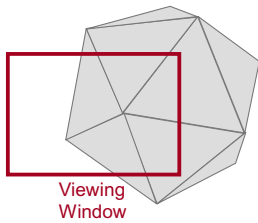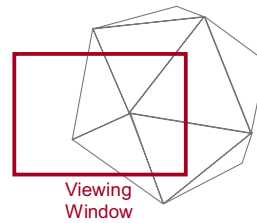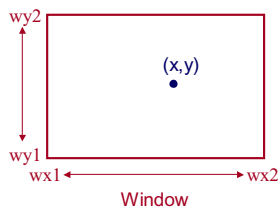
Viewing
Window

Clipping

- Avoid drawing parts of primitives outside window
  - o Points
  - o Lines
  - o Polygons
  - o Circles
  - o etc.

Viewing
Window

Point Clipping

- Is point (x,y) inside the clip window?

wy2

(x,y)

wy1

wx1

wx2

Window

```
inside =
  (x >= wx1) &&
  (x <= wx2) &&
  (y >= wy1) &&
  (y <= wy2);
```

Line Clipping
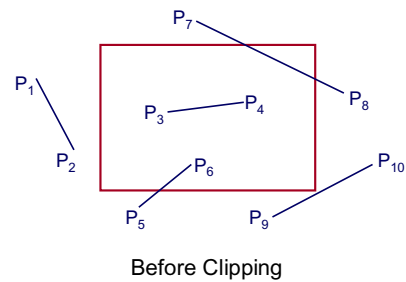
- Find the part of a line inside the clip window

P_7
P_1
P_3 P_4 P_8
P_2
P_6 P_{10}
P_5 P_9

Before Clipping

Line Clipping

- Find the part of a line inside the clip window

P'_7
P'_8
P_3 P_4
P_6
P'_5

After Clipping
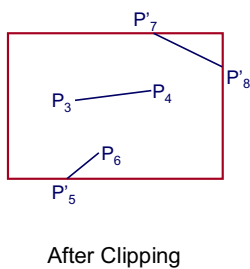
Cohen Sutherland Line Clipping

- Use simple tests to classify easy cases first

P_7
P_1
P_3 P_4 P_8
P_2
P_6 P_{10}
P_5 P_9

Cohen Sutherland Line Clipping

- Classify some lines quickly by AND of bit codes representing regions of two endpoints (must be 0)

```
1001            P_7 0001        0101
                                        Bit 4
  P_1
1000      P_3  0000   P_4      P_8
  P_2                          0100
                 P_6
                               P_10
                                        Bit 3
1010      P_5   0010   P_9      0110
     Bit 1           Bit 2
```

Cohen Sutherland Line Clipping

- Classify some lines quickly by AND of bit codes representing regions of two endpoints (must be 0)

```
1001            P_7 0001        0101
                                        Bit 4
  P_1
1000      P_3  0000   P_4      P_8
  P_2                          0100
                 P_6
                               P_10
                                        Bit 3
1010      P_5   0010   P_9      0110
     Bit 1           Bit 2
```

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                               0100
                 P_6
                               P_10
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1010      P_5   0010   P_9      0110
     Bit 1           Bit 2
```

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1001            P_7 0001        0101
                                        Bit 4
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                               0100
                 P_6
                               P_10
                                        Bit 3
1010      P_5   0010   P_9      0110
     Bit 1           Bit 2
```
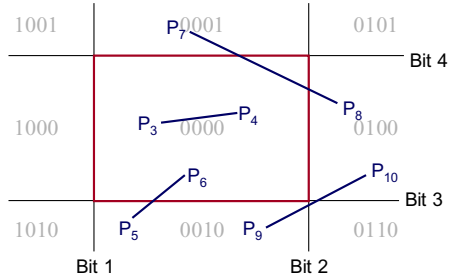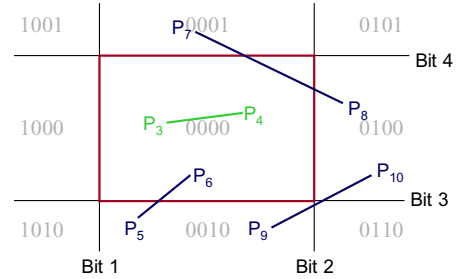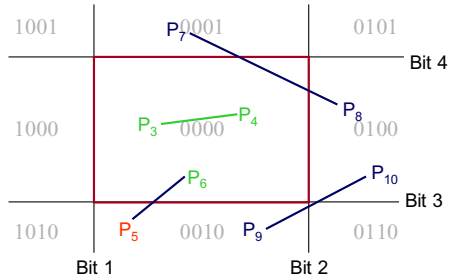
Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly

```
1001            P_7 0001        0101
                                        Bit 4
1000      P_3  0000   P_4      P_8
                               0100
                 P_6
                               P_10
                                        Bit 3
1010      P_5   0010   P_9      0110
     Bit 1           Bit 2
```

Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly

```
1001            P_7 0001        0101
                                        Bit 4
1000      P_3  0000   P_4      P_8
                               0100
                 P_6
                               P_10
                                        Bit 3
1010      P_5   0010   P_9      0110
     Bit 1           Bit 2
```
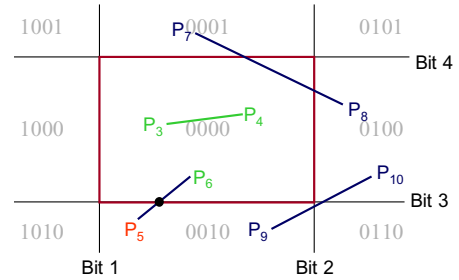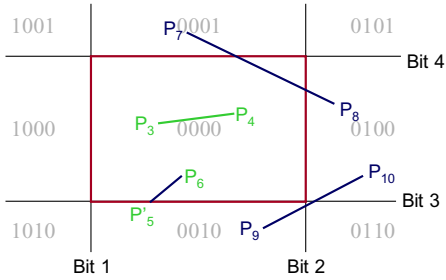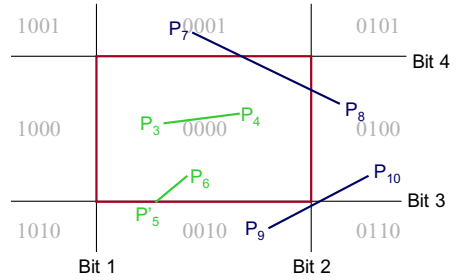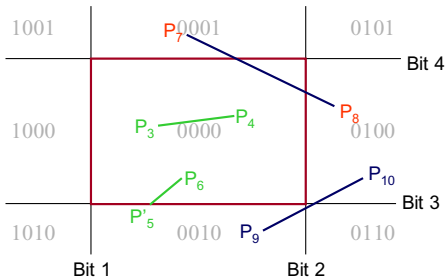
Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly

Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly
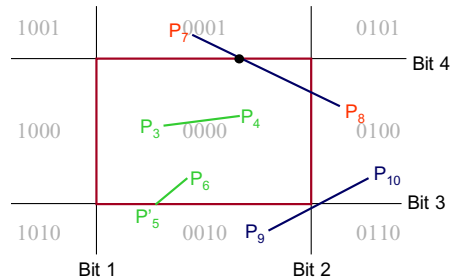
Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly

Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly

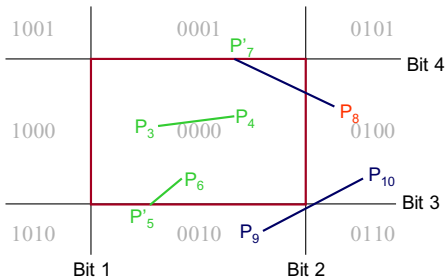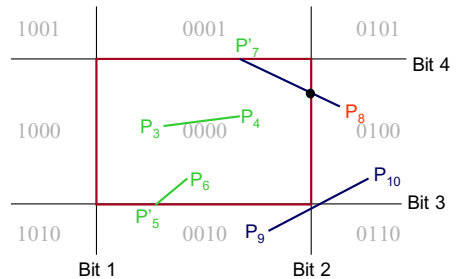## Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly
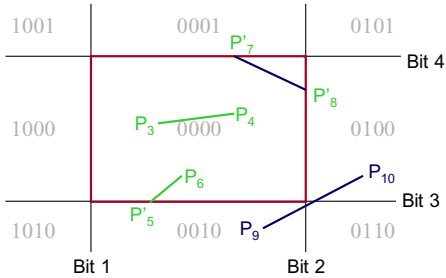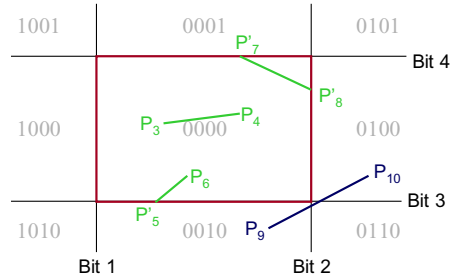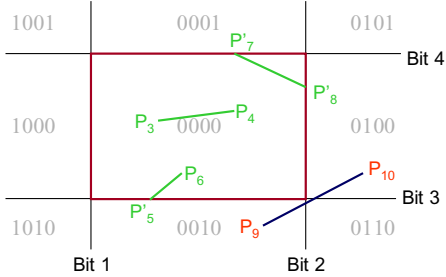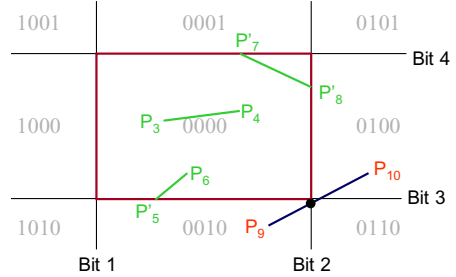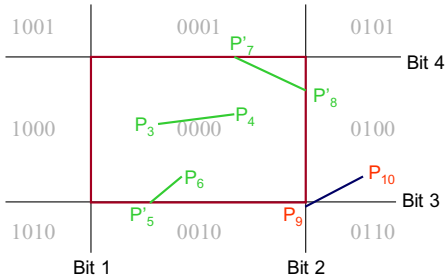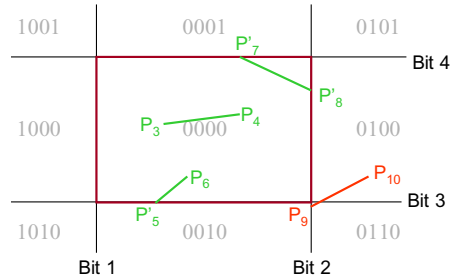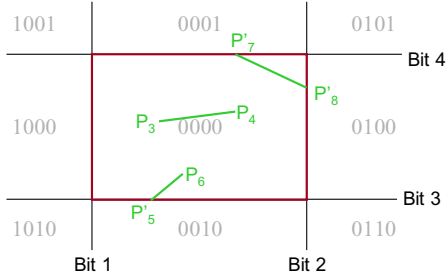
Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly

Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly

1001   0001   0101
P'_7 — Bit 4
P'_8
1000 P_3 0000 P_4 0100
P_6 P_{10}
P'_5 — Bit 3
1010   0010 P_9 0110
Bit 1   Bit 2

Cohen-Sutherland Line Clipping

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Cohen-Sutherland Line Clipping

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P'_5 — Bit 3
1010   0010 P_9 0110
Bit 1   Bit 2
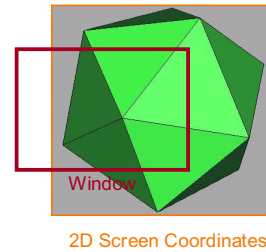
Cohen-Sutherland Line Clipping

- Compute interesections with window boundary for lines that can't be classified quickly
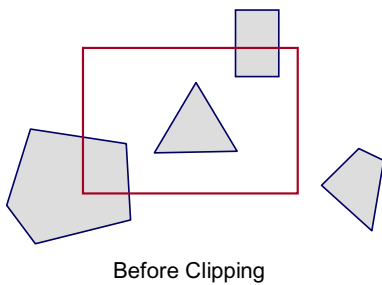
Clipping

- Avoid drawing parts of primitives outside window
  - o Points
  - o Lines
  - o Polygons
  - o Circles
  - o etc.

Window
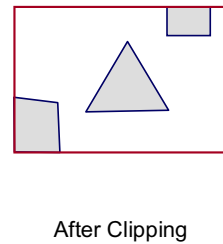
2D Screen Coordinates

Polygon Clipping

- Find the part of a polygon inside the clip window?
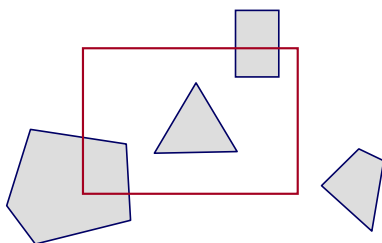

Before Clipping

Polygon Clipping

- Find the part of a polygon inside the clip window?

After Clipping
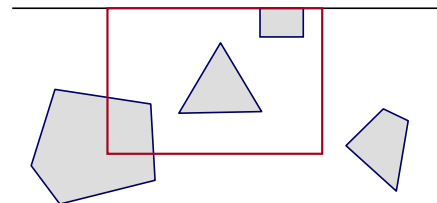
Sutherland Hodgeman Clipping

- Clip to each window boundary one at a time

Sutherland Hodgeman Clipping

- Clip to each window boundary one at a time

Sutherland Hodgeman Clipping

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Sutherland Hodgeman Clipping

- Clip to each window boundary one at a time

Sutherland Hodgeman Clipping

- Clip to each window boundary one at a time

Clipping to a Boundary

- Do inside test for each point in sequence,
  Insert new points when cross window boundary,
  Remove points outside window boundary

Window Boundary

Inside
Outside

P_2 P_1

P_3

P_5

P_4

Clipping to a Boundary

- Do inside test for each point in sequence,
  Insert new points when cross window boundary,
  Remove points outside window boundary

Window Boundary

Inside
Outside

P_2 P_1

P_3

P_5

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Window Boundary

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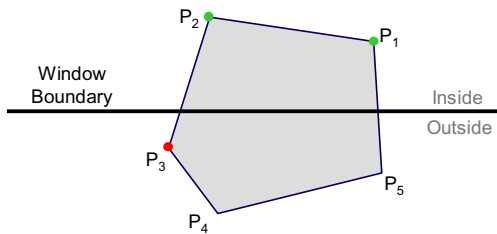 Remove points outside window boundary

Clipping to a Boundary

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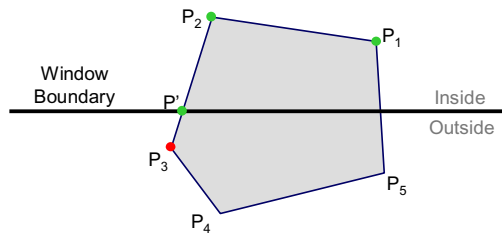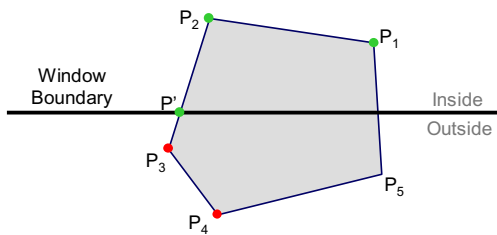 Remove points outside window boundary
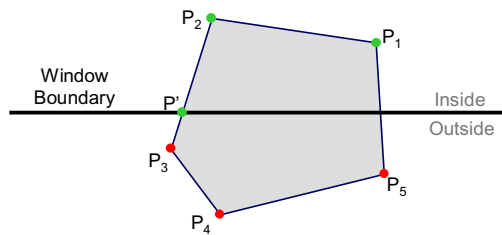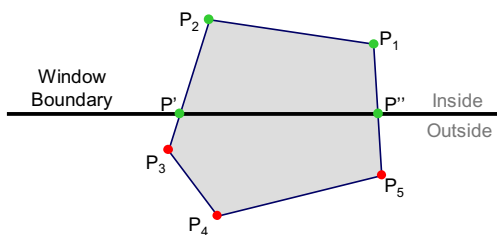
Clipping to a Boundary

- Do inside test for each point in sequence,
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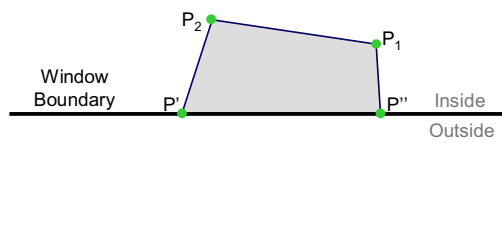## Clipping to a Boundary

- Do inside test for each point in sequence,
  Insert new points when cross window boundary,
  Remove points outside window boundary
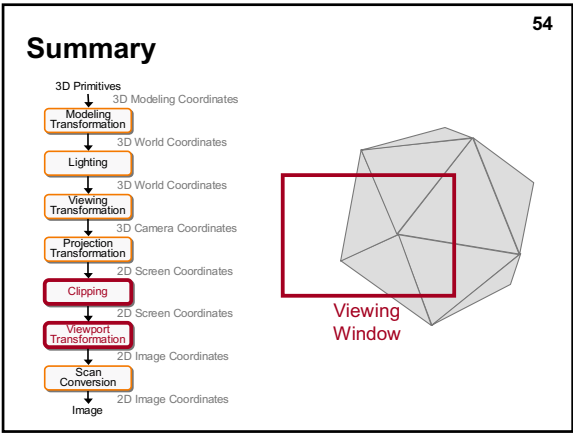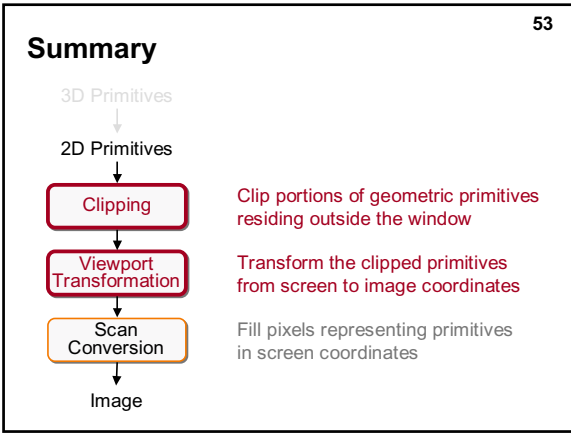
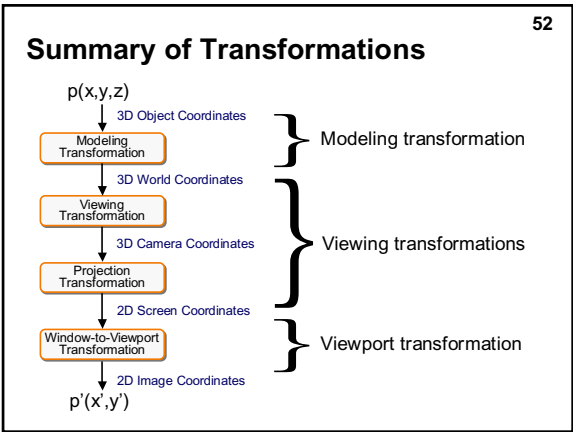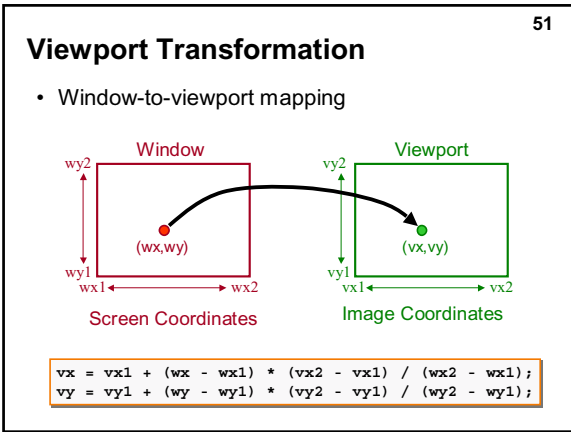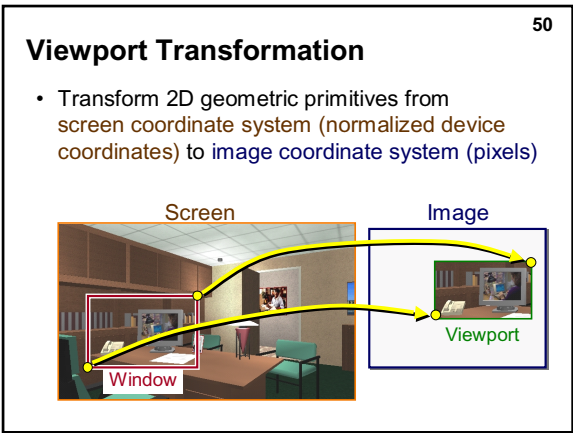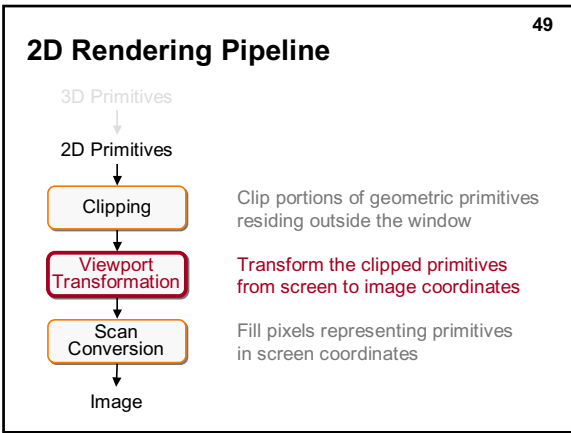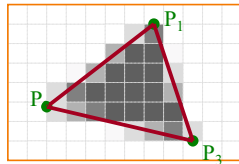## 2D Rendering Pipeline

3D Primitives

↓

2D Primitives

↓

Clipping — Clip portions of geometric primitives residing outside the window

↓

Viewport Transformation — Transform the clipped primitives from screen to image coordinates

↓

Scan Conversion — Fill pixels representing primitives in screen coordinates

↓

Image

Viewport Transformation

- Transform 2D geometric primitives from screen coordinate system (normalized device coordinates) to image coordinate system (pixels)

Screen | Image

Window

Viewport

Viewport Transformation

- Window-to-viewport mapping

Window: wy2, wy1, wx1, wx2, (wx,wy) — Screen Coordinates

Viewport: vy2, vy1, vx1, vx2, (vx,vy) — Image Coordinates

```
vx = vx1 + (wx - wx1) * (vx2 - vx1) / (wx2 - wx1);
vy = vy1 + (wy - wy1) * (vy2 - vy1) / (wy2 - wy1);
```

Summary of Transformations

$p(x,y,z)$

↓ 3D Object Coordinates

Modeling Transformation — } Modeling transformation

↓ 3D World Coordinates

Viewing Transformation

↓ 3D Camera Coordinates

Projection Transformation — } Viewing transformations

↓ 2D Screen Coordinates

Window-to-Viewport Transformation — } Viewport transformation

↓ 2D Image Coordinates

$p'(x',y')$

Summary

3D Primitives

↓

2D Primitives

↓

Clipping — Clip portions of geometric primitives residing outside the window

↓

Viewport Transformation — Transform the clipped primitives from screen to image coordinates

↓

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↓

Image

Summary

3D Primitives

3D Modeling Coordinates

Modeling Transformation

3D World Coordinates

Lighting

3D World Coordinates

Viewing Transformation

3D Camera Coordinates

Projection Transformation

2D Screen Coordinates

Clipping

2D Screen Coordinates

Viewport Transformation

2D Image Coordinates

Scan Conversion

2D Image Coordinates

Image

Viewing Window

Next Time

3D Primitives

↓ 3D Modeling Coordinates

Modeling Transformation

↓ 3D World Coordinates

Lighting

↓ 3D World Coordinates

Viewing Transformation

↓ 3D Camera Coordinates

Projection Transformation

↓ 2D Screen Coordinates

Clipping

↓ 2D Screen Coordinates

Viewport Transformation

↓ 2D Image Coordinates

Scan Conversion

↓ 2D Image Coordinates

Image

Scan Conversion!