Probability and Information Retrieval

Introduction to Artificial Intelligence
COS302
Michael L. Littman
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Administration

Foundations of Statistical Natural Language Processing
By Christopher D. Manning and Hinrich Schutze

Grade distributions online.

The IR Problem

query
- doc1
- doc2
- doc3

...

Sort docs in order of relevance to query.

Example Query

Query: The 1929 World Series
384,945,633 results in Alta Vista
- GNU's Not Unix! - the GNU Project and the Free Software Foundation (FSF)
- Yahoo! Singapore
- The USGenWeb Project - Home Page
- ...

Better List (Google)

- TSN Archives: The 1929 World Series
- Baseball Almanac - World Series Menu
- 1929 World Series - PHA vs. CHC - Baseball-Reference.com
- World Series Winners (1903-1929) (Baseball World)

Goal

Should return as many relevant docs as possible
recall
Should return as few irrelevant docs as possible
precision
Typically a tradeoff...

Main Insights

How identify "good" docs?

- More words in common is good.
- Rare words more important than common words.
- Long documents carry less weight, all other things being equal.

Bag of Words Model

Just pay attention to which words appear in document and query.

Ignore order.

Boolean IR

"and" all uncommon words

Most web search engines.

- Altavista: 79,628 hits
- fast
- not so accurate by itself

Example: Biography

Science and the Modern World (1925), a series of lectures given in the United States, served as an introduction to his later metaphysics.

Whitehead's most important book, *Process and Reality* (1929), took this theory to a level of even greater generality.

http://www-groups.dcs.st-and.ac.uk/~history/Mathematicians/Whitehead.html

Vector-space Model

For each word in common between document and query, compute a weight. Sum the weights.

tf = (term frequency) number of times term appears in the document

idf = (inverse document frequency) divide by number of times term appears in any document

Also various forms of document-length normalization.

Example Formula

i	$\text{sum}_j\ tf_{i,j}$	df_i
Insurance	10440	3997
Try	10422	8760

Weight(i,j) = $(1+\log(tf_{i,j}))\ \log N/df_i$

Unless $tf_{i,j} = 0$ (then 0).

N documents, df_i doc frequency

Cosine Normalization

Cos(q,d) = sum_i q_i d_i /
sqrt(sum_i q_i^2) sqrt(sum_i d_i^2)

Downweights long documents.
(Perhaps too much.)

Probabilistic Approach

Lots of work studying different weighting schemes.

Often very *ad hoc*, empirically motivated.

Is there an analog of A* for IR? Elegant, simple, effective?

Language Models

Probability theory is gaining popularity. Originally speech recognition:

If we can assign probabilities to sentence and phonemes, we can choose the sentence that minimizes the chance that we're wrong…

Probability Basics

Pr(A): Probability A is true

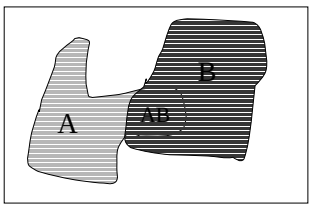
Pr(AB): Prob. both A & B are true

Pr(~A): Prob. of not A: 1-Pr(A)

Pr(A|B): Prob. of A given B
Pr(AB)/Pr(B)

Pr(A+B): Probability A or B is true
Pr(A) + Pr(B) – Pr(AB)

Venn Diagram



Bayes Rule

Pr(A|B) = Pr(B|A) Pr(A) / Pr(B)
because
Pr(AB) = Pr (B) Pr(A|B) = Pr(B|A) Pr(A)

The most basic form of "learning":

- picking a likely model given the data
- adjusting beliefs in light of new evidence

Probability Cheat Sheet

Chain rule:

$Pr(A,X|Y) = Pr(A|Y)\ Pr(X|A,Y)$

Summation rule:

$Pr(X|Y) = Pr(A\ X\ |\ Y) + Pr(\sim A\ X\ |\ Y)$

Bayes rule:

$Pr(A|BX) = Pr(B|AX)\ Pr(A|X)/Pr(B|X)$

Speech Example

$Pr(\text{sentence}|\text{phonemes})$

$= Pr(\text{phonemes}|\text{sentence})\ Pr(\text{sentence}) / Pr(\text{phonemes})$

Constant

Pronunciation model

Language model

Classification Example

Given a song title, guess if it's a country song or a rap song.

- U Got it Bad
- Cowboy Take Me Away
- Feelin' on Yo Booty
- When God-Fearin' Women Get The Blues
- God Bless the USA
- Ballin' out of Control

Probabilistic Classification

Language model gives:

- $Pr(T|R)$, $Pr(T|C)$, $Pr(C)$, $Pr(R)$

Compare

- $Pr(R|T)$ vs. $Pr(C|T)$
- $Pr(T|R)\ Pr(R) / Pr(T)$ vs. $Pr(T|C)\ Pr(C) / Pr(T)$
- $Pr(T|R)\ Pr(R)$ vs. $Pr(T|C)\ Pr(C)$

Naïve Bayes

$Pr(T|C)$

Generate words independently

$Pr(w_1\ w_2\ w_3\ \ldots\ w_n|C)$

$= Pr(w_1|C)\ Pr(w_2|C)\ \ldots\ Pr(w_n|C)$

So, $Pr(\text{party}|R) = 0.02$, $Pr(\text{party}|C) = 0.001$

Estimating Naïve Bayes

Where would these numbers come from?

Take a list of country song titles.

First attempt:

$Pr(w|C) = count(w; C) / sum_w\ count(w; C)$

Smoothing

Problem: Unseen words.
Pr(party|C) = 0

Pr(Even Party Cowboys Get the Blues) = 0

Laplace Smoothing:

Pr(w|C) = (1+count(w; C))
/ sum_w (1+count(w; C))

Other Applications

Filtering
- Advisories

Text classification
- Spam vs. important
- Web hierarchy
- Shakespeare vs. Jefferson
- French vs. English

IR Example

Pr(d|q) = Pr(q|d) Pr(d) / Pr(q)

Language model

Constant

Prior belief d is relevant (assume equal)

Can view each document like a category for classification.

Smoothing Matters

p(w|d) =
p_s(w|d) if count(w;d)>0 (seen)
p(w|collection) if count(w;d)=0

p_s(w|d): estimated from document and smoothed

p(w|collection): estimated from corpus and smoothed

Equivalent effect to TF-IDF.

What to Learn

IR problem and TF-IDF.

Unigram language models.

Naïve Bayes and simple Bayesian classification.

Need for smoothing.

Homework 6 (due 11/14)

1. Use the web to find sentences to support the analogy traffic:street::water:riverbed. Give the sentences and their sources.
2. Two common Boolean operators in IR are "and" and "or". (a) Which would you choose to improve recall? (b) Which would you use to improve precision?

Homework 6 (cont'd)

3. **Argue that the language modeling approach to IR gives an effect like TF-IDF. (a) First, argue that Pr(q|d) > Pr(q'|d) if q' is just like q but**